

Data Structures – CST 201

Module - 2

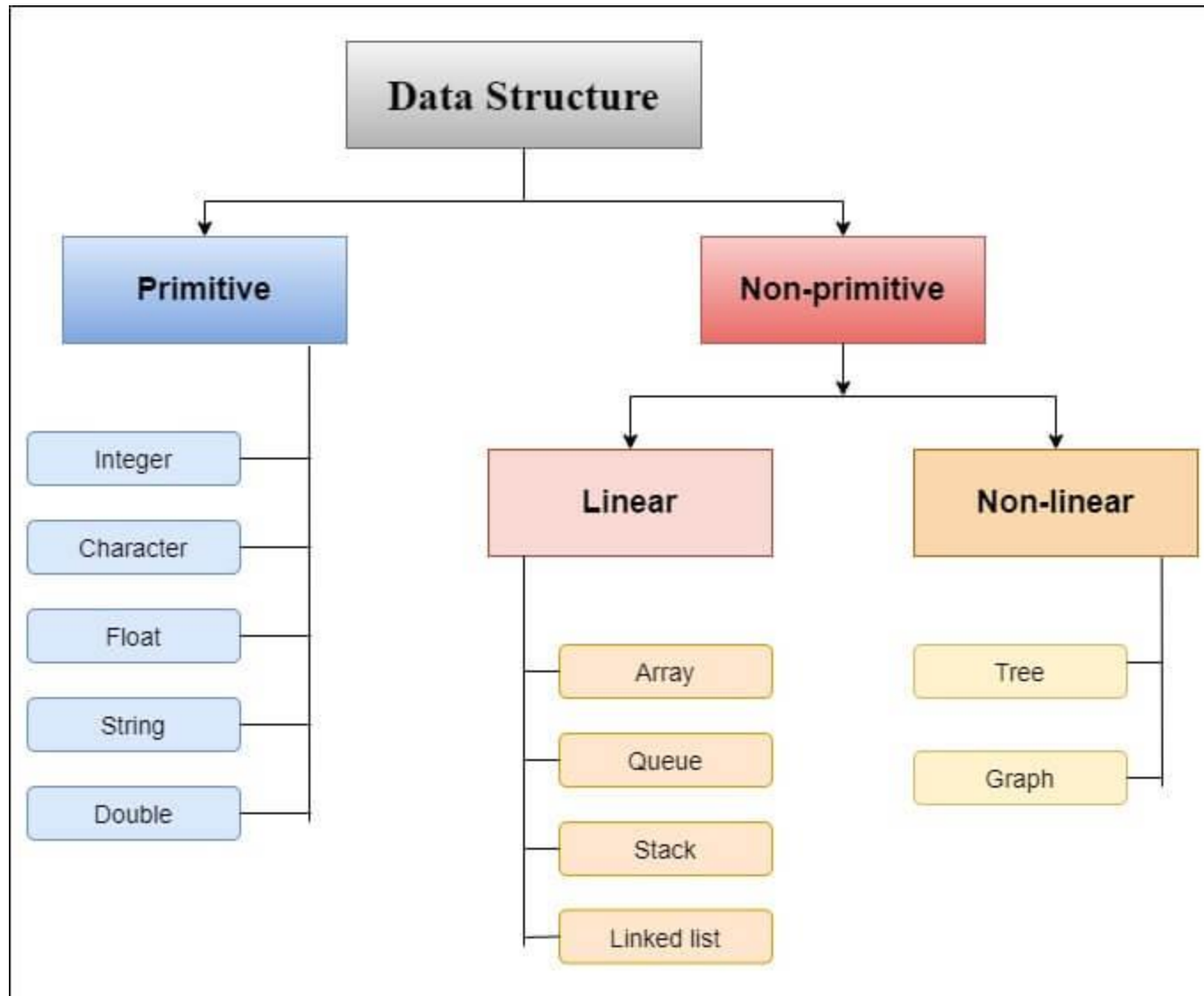
Syllabus

- Polynomial representation using Arrays
- Sparse matrix
- Stacks
 - Evaluation of Expressions
- Queues
 - Circular Queues
 - Priority Queues
 - Double Ended Queues,
- Linear Search
- Binary Search

DATA STRUCTURES

- Data may be organized in many different ways
- The logical or mathematical model of a particular organization of data is called data structure
- A data structure is a particular way of organizing data in a computer so that it can be used efficiently
- It is also called building block of a program.

TYPE DATA STRUCTURES



TYPE DATA STRUCTURES

- **Primitive data structure(Simple Data structure)**
 - Simple data structure can be constructed with the help of primitive data types
 - It can hold a single value
- **Non-primitive data structure(Compound data structure)**
 - It can be constructed with the help of any one of the primitive data structure and it is having a specific functionality. It is divided into two.
 - **Linear data structure**
 - Elements are arranged in a sequential manner
 - **Non-linear data structure**
 - Elements are arranged in a random manner

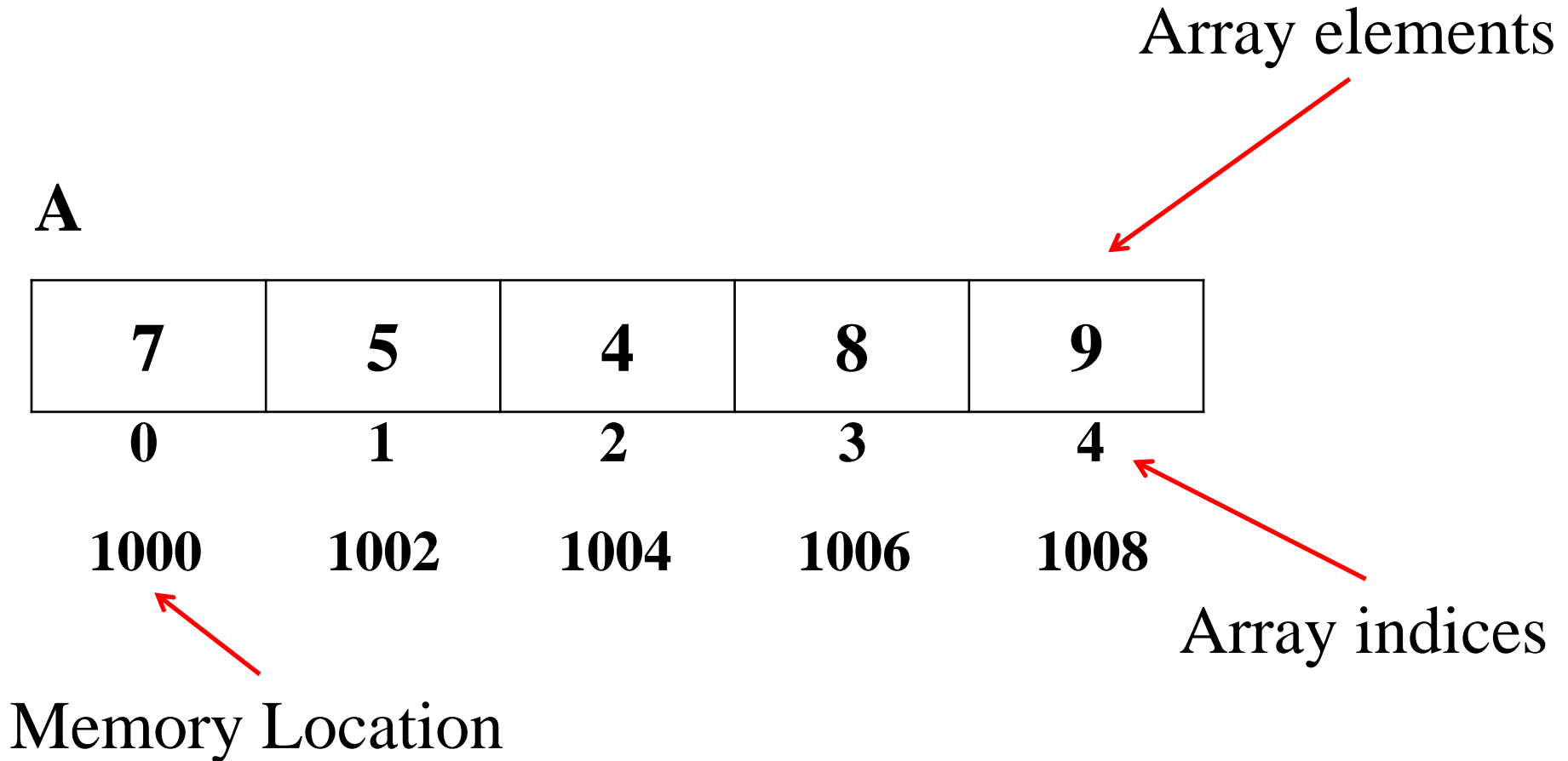
OPERATIONS ON DATA STRUCTURES

- Add an element
- Delete an element
- Traverse / Display
- Sort the list of elements
- Search for a data element

ARRAY

- It is a Linear data structure
- It is a list of finite no. of homogeneous data elements
 - It is finite, because it contains fixed no. of elements
 - It is homogeneous, because the elements of the array are of same data types (int, float, double, char, etc)
- Array is a collection of similar items stored at contiguous memory locations
- Elements can be accessed randomly using indices of an array

ARRAY



NB: Array index will always starts with 0

ARRAY - TERMINOLOGIES

- **Type:** Kind of data type it is meant for.
- **Base:** Address of the memory location where the first element of the array is located
- **Index:** Subscript like A_i or $A[i]$
- **Range of indices:** Boundaries of an array
 - Upper bound(U) and lower bound(L)
 - In C, the range of indices is from 0
- **Index ($A[i]$) = $L + i - 1$**
- **Size(Length/Dimension):** The no. of elements in an array.
 - $\text{Size}(A) = U - L + 1$

ARRAY

- Different Types
 - Single Dimensional Array

A

4	5	7	8	10
0	1	2	3	4

- Multidimensional Array

A

		Columns		
		0	1	2
rows	0	A[0][0]	A[0][1]	A[0][2]
	1	A[1][0]	A[1][1]	A[1][2]

Representation of Array in Memory

```
int a[10]={3,45,24,56,34,23,7,29,66,76}
```

Address	2000	2002	2004	2006	2008	2010	2012	2014	2016	2018
	3	45	24	56	34	23	7	29	66	76
Index	0	1	2	3	4	5	6	7	8	9

```
char mystring="INDIA"
```

2000	2001	2002	2003	2004
I	N	D	I	A
0	1	2	3	4

The basic Operations Performed in an Array

- Traversal
 - Processing each element in the list
- Insertion
 - Adding a new element to the list
- Deletion
 - Removing an element from the list
- Searching
 - Find the location of the element with the given value
- Sorting
 - Arranging elements in some type of order
- Merging
 - Combining two list into a single list

Array Traversal

- In traversing operation of an array, each element of an array is accessed exactly for once for processing.
- This is also called visiting of an array.
- If we need to print all the elements or to count no. of elements or to find largest or smallest element, the traversal should be done.

TRAVERSING

ALGORITHM

1. Start
2. Set $K=LB$
3. Repeat step 3 and 4 until $K \leq UB$
4. Apply Process to Array
5. Increase Counter $K=K+1$
6. Stop

Program

```
#include <stdio.h>

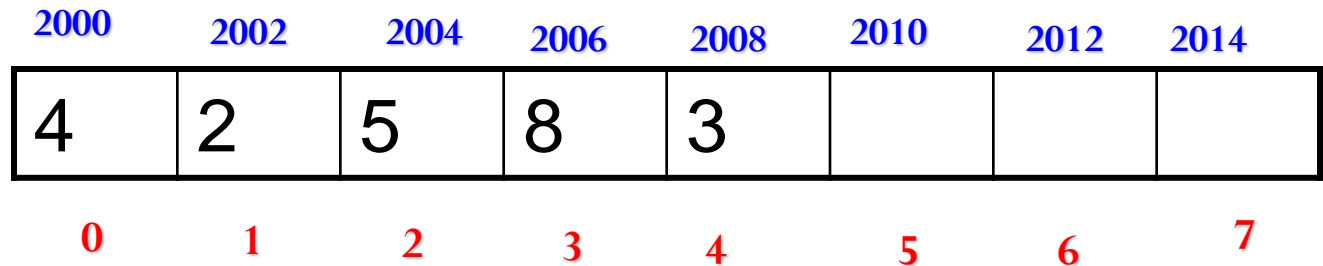
void main()
{
int LA[] = {2,4,6,8,9};
int i, n = 5;
printf("The array elements are:\n");
for(i = 0; i < n; i++)
{
printf("LA[%d] = %d \n", i, LA[i]);
}
}
```

INSERTION

- Insert operation is to insert one or more data elements into an array.
- Based on the requirement, new element can be added at the beginning, end or any given index of array.
- Insertion at the end of the array can be easily done
- Suppose we need to insert an element at the middle of the array
 - Half of the elements must be moved forward to the new location to accommodate the new element and keep the order of other elements

`int a[8]={4,2,5,8,3}`

UB=4, LB=0



ALGORITHM

1. Start
2. Let `a[]` be an array
3. Let `J=UB`

PROGRAM

```
#include <stdio.h>
void main()
{
int a[8] = {4,2,5,8,3};
int J=4;
```

Suppose we need to insert an element 9 to the position 2

Suppose we need to insert an element 9 to the position 2

```
int a[8]={4,2,5,8,3}
```

2000	2002	2004	2006	2008	2010	2012	2014
4	2	5	8	3			
0	1	2	3	4	5	6	7

ALGORITHM

1. Start
2. Let a[] be an array
3. J
4. Let J=UB
5. Let ITEM be the new element and position is K

PROGRAM

```
#include <stdio.h>
void main()
{
int a[8] = {4,2,5,8,3};
int J=4;
Int item=9,K=2;
```

Suppose we need to insert an element 9 to the position 2

`int a[8] = {4, 2, 5, 8, 3}`

	2000		2002		2004		2006		2008		2010		2012		2014
	4		2		5		8		3						
	0		1		2		3		4		5		6		7

Suppose we need to insert an element 9 to the position 2

`int a[8]={4,2,5,8,3}`

Step 1: Need to create space for position 2

	2000		2002		2004		2006		2008		2010		2012		2014
4		2		5		8		3							
0		1		2		3		4		5		6		7	

Step 2: First shift last element 3 to position 5

That is `a[5]=a[4]`

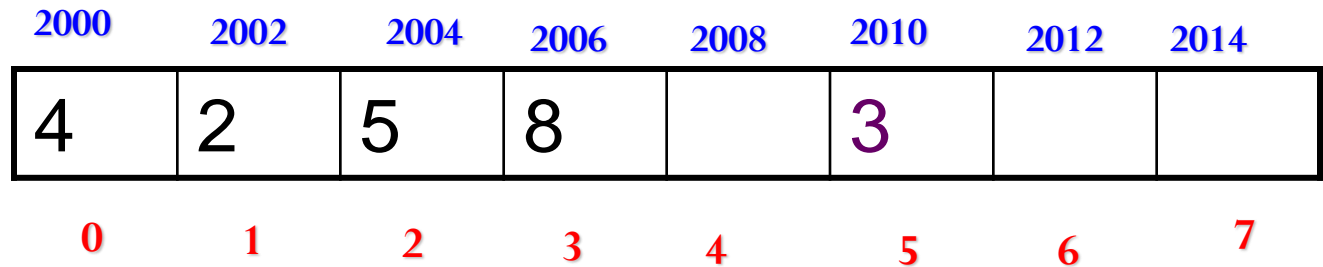
Step 2: First shift last element 3 to position 5

That is $a[5]=a[4]$

`int a[8]={4,2,5,8,3}`

	2000	2002	2004	2006	2008	2010	2012	2014
	4	2	5	8		3		
	0	1	2	3	4	5	6	7

`int a[8] = {4, 2, 5, 8, 3}`



Step 3: Now we have a space to shift 8 to position 4

That is $a[4] = a[3]$

Step 3: Now we have a space to shift 8 to position 4

That is $a[4]=a[3]$

`int a[8]={4,2,5,8,3}`

2000	2002	2004	2006	2008	2010	2012	2014
4	2	5		8	3		
0	1	2	3	4	5	6	7

Step 4: Now we have a space to shift 5 to position 3

That is $a[3]=a[2]$

Step 4: Now we have a space to shift 5 to position 3

That is $a[3]=a[2]$

`int a[8]={4,2,5,8,3}`

2000	2002	2004	2006	2008	2010	2012	2014
4	2		5	8	3		
0	1	2	3	4	5	6	7

Step 4: Now position 2 is free

So that we can insert item to position 2

Step 5: Now position 2 is free

So that we can insert item to position 2

```
int a[8]={4,2,5,8,3}
```

2000	2002	2004	2006	2008	2010	2012	2014
4	2	9	5	8	3		
0	1	2	3	4	5	6	7

4

2

9

5

8

3

ALGORITHM

1. Start
2. Let $a[]$ be an array
3. Let $J=UB$
4. Let ITEM be the new element and position is K
5. Repeat step 6 & 7 while $J \geq K$
6. Set $a[J+1]=a[J]$
7. Set $J=J-1$
8. Set $a[K]=ITEM$
9. Set $UB=UB+1$
10. Stop

PROGRAM

```
#include <stdio.h>
void main()
{
int a[8] = {4,2,5,8,3},n=4;
int j=n, item=9,k=2,i;
printf("Orginal array is");
for (i=0;i<=n;i++)
    printf("%d ",a[i]);
while(j>=k)
    a[j+1]=a[j];
    j--;
a[k]=item;
n=n+1;
printf("New array is");
for(i=0;i<=n;i++)
    printf("%d",a[i]);
getch();
}
```

DELETION

- Deletion refers to removing an existing element from the array and re-organizing all elements of an array.
- Deleting an element at the end of the array presents no difficulties
- But deleting an element somewhere in the middle of the array would require that each subsequent element be moved one location backward to fill up the location

`int a[8]={4,2,5,8,3,9,7}`

UB=6, LB=0

2000	2002	2004	2006	2008	2010	2012	2014
4	2	5	8	3	9	7	
0	1	2	3	4	5	6	7

ALGORITHM

1. Start
2. Let `a[]` be an array
3. Let `J=UB`

PROGRAM

```
#include <stdio.h>
void main()
{
int a[8] = {4,2,5,8,3,9,7};
int J=6;
```

Suppose we need to delete an element 5 from the position 2

Suppose we need to delete an element 5 from the position 2

```
int a[8]={4,2,5,8,3,9,7}
```

UB=6, LB=0

2000	2002	2004	2006	2008	2010	2012	2014
4	2	5	8	3	9	7	
0	1	2	3	4	5	6	7

Actually we are not deleting the item in position 2, we are just overwriting the elements in position 2 with position 3 and position 3 with position 4 and position 4 with position 5 and position 5 with position 6 and change UB to UB-1

`int a[8]={4,2,5,8,3,9,7}`

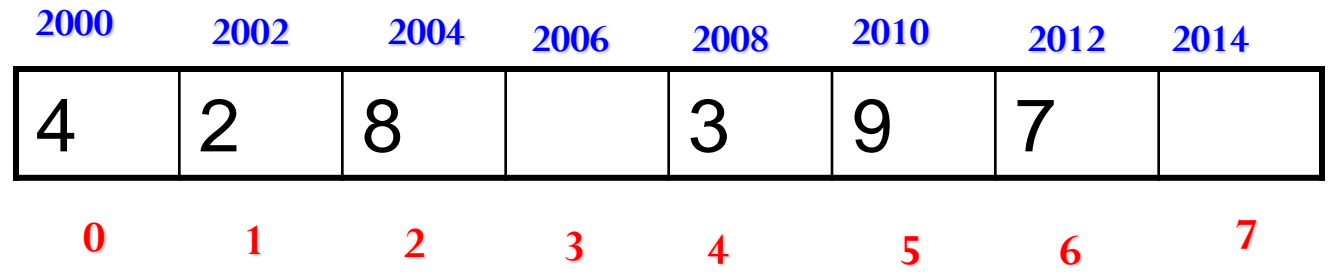
`UB=6, LB=0`

2000	2002	2004	2006	2008	2010	2012	2014
4	2	5	8	3	9	7	
0	1	2	3	4	5	6	7

`a[2]=a[3]`

`int a[8]={4,2,5,8,3,9,7}`

UB=6, LB=0

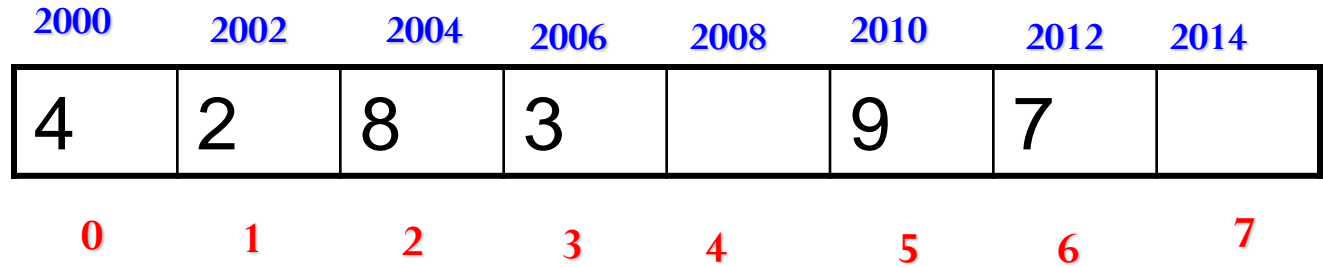


`a[2]=a[3]`

`a[3]=a[4]`

`int a[8]={4,2,5,8,3,9,7}`

UB=6, LB=0



`a[2]=a[3]`

`a[3]=a[4]`

`a[4]=a[5]`

`int a[8]={4,2,5,8,3,9,7}`

UB=6, LB=0

2000	2002	2004	2006	2008	2010	2012	2014
4	2	8	3	9		7	
0	1	2	3	4	5	6	7

`a[2]=a[3]`

`a[3]=a[4]`

`a[4]=a[5]`

`a[5]=a[6]`

`int a[8]={4,2,5,8,3,9,7}`

`UB=6, LB=0`

2000	2002	2004	2006	2008	2010	2012	2014
4	2	8	3	9	7		
0	1	2	3	4	5	6	7

`a[2]=a[3]`

`a[3]=a[4]`

`a[4]=a[5]`

`a[5]=a[6]`

`UB=UB-1`

ALGORITHM

1. Start
2. Let a[] be an array
3. Let k be the position of the element to be deleted
4. Set item=a[k]
5. Repeat step 6 & 7 for J=k to UB-1
6. Set a[J]=a[J+1]
7. Set J=J+1
8. Set UB=UB-1
9. Stop

PROGRAM

```
#include <stdio.h>
void main()
{
int a[8] = {4,2,5,8,3,9,7},n=6;
int j, item,k=2,i;
Item=a[k];
Printf("Orginal array is");
For (i=0;i<=n;i++)
    printf("%d ",a[i]);
For(j=k;j<n;j++)
    a[j]=a[j+1];
n=n-1;
Printf("New array is");
For(i=0;i<=n;i++)
    printf("%d",a[i]);
getch();
}
```

Linear Search

7	5	4	8	9
0	1	2	3	4

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=8

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=8

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=8

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=8

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=8

Stop searching

Print “Search data found”

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=1

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=1

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=1

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=1

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=1

Linear Search

7	5	4	8	9
0	1	2	3	4

Search Data=1

Print “Search data not found”

Algorithm SEARCH_ARRAY(KEY)

Input: KEY is the element to be searched.

Output: Index of KEY in A or a message on failure.

Data structures: An array A[L ... U]. //L and U are the lower and upper bound of array index

Steps:

1. $i = L$, found = 0, location = 0 //found = 0 indicates search is not finished and unsuccessful
2. While ($i \leq U$) and (found = 0) do // Continue if all or any one condition do(es) not satisfy
 1. If COMPARE(A[i], KEY) = TRUE then //If key is found
 1. found = 1 //Search is finished and successful
 2. location = i
 2. Else
 1. $i = i + 1$ //Move to the next
 3. EndIf
3. EndWhile
4. If found = 0 then
 1. Print "Search is unsuccessful : KEY is not in the array"
5. Else
 1. Print "Search is successful : KEY is in the array at location", location
6. EndIf
7. Return(location)
8. Stop

Linear Search- Algorithm

Algorithm LinearSearch()

```
{    Read  $n$ , the size of array
    Read the elements of  $A[]$ 
    Read the search data  $search\_data$ 
    flag=0
    for i=0 to n-1 do
    {    if  $A[i]== search\_data$  then
        {    flag=1
            break
        }
    }
    if  $flag==0$  then
        Print "Search data not found"
    else
        Print "Search data found at the index i"
}
```


Linear Search- Program

```
void main()
{
    int A[3],n,i,search_data,flag=0;
    printf("Enter the number of elements: ");
    scanf("%d",&n);
    printf("Enter %d numbers ",n);
    for(i=0;i<n;i++)
        scanf("%d",&A[i]);
    printf("Enter Search Data: ");
    scanf("%d",&search_data);
    for(i=0;i<n;i++)
    {
        if(A[i]==search_data)
        {
            flag=1;
            break;
        }
    }
    if(flag==0)
        printf("Search data not found");
    else
        printf("Search data found at the index %d",i);
}
```

POLYNOMIAL REPRESENTATION USING ARRAY

- Example Polynomial is

$$A(x) = 3x^2 + 2x + 4 \text{ and}$$

$$B(x) = x^4 + 10x^3 + 3x^2 + 1$$

- For a mathematician a polynomial is a sum of terms where each term has the form

$$ax^e$$

- x is the variable,
- a is the coefficient and
- e is the exponent.
- However this is not an appropriate definition for our purposes.
- When defining a data object one must decide what functions will be available, what their input is, what their output is and exactly what it is that they do.

POLYNOMIAL REPRESENTATION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$

POLYNOMIAL REPRESENTATION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$

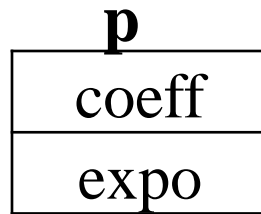
```
struct poly
{
    int coeff;
    int expo;
}p;
```

POLYNOMIAL REPRESENTATION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$

struct poly

```
{  
    int coeff;  
    int expo;  
}p;
```



POLYNOMIAL REPRESENTATION USING ARRAY

■ $7x^4 + 3x^2 + 2x + 4$

```
struct poly
{
    int coeff;
    int expo;
}p[10];
```

p

0	coeff-1
	expo-1
1	coeff-2
	expo-2
	.
	.
	.
	.
	.
9	coeff-10
	expo-10

POLYNOMIAL REPRESENTATION USING ARRAY

■ $7x^4 + 3x^2 + 2x + 4$

```
struct poly
{
    int coeff;
    int expo;
}p[10];
```

	p
0	7
	4
1	3
	2
2	2
	1
3	4
	0
	.
	.
9	.

POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

```
struct poly
{
    int coeff;
    int expo;
}p1[10],p2[10],p3[10];
```

POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

```

struct poly
{
    int coeff;
    int expo;
}p1[10],p2[10],p3[10];
    
```

p1

0	7
	4
1	3
	2
2	2
	1
3	4
	0
	.
	.
9	.

p2

0	5
	3
1	4
	2
2	
3	
	.
	.
9	.

p3

0	
1	
2	
3	
4	

POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

```
struct poly
{
    int coeff;
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```

p1

	7
0	4
	3
1	2
	2
2	1
	4
3	0
	.
	.
9	.

p2

	5
0	3
	4
1	2
2	
3	
	.
	.
9	.

p3

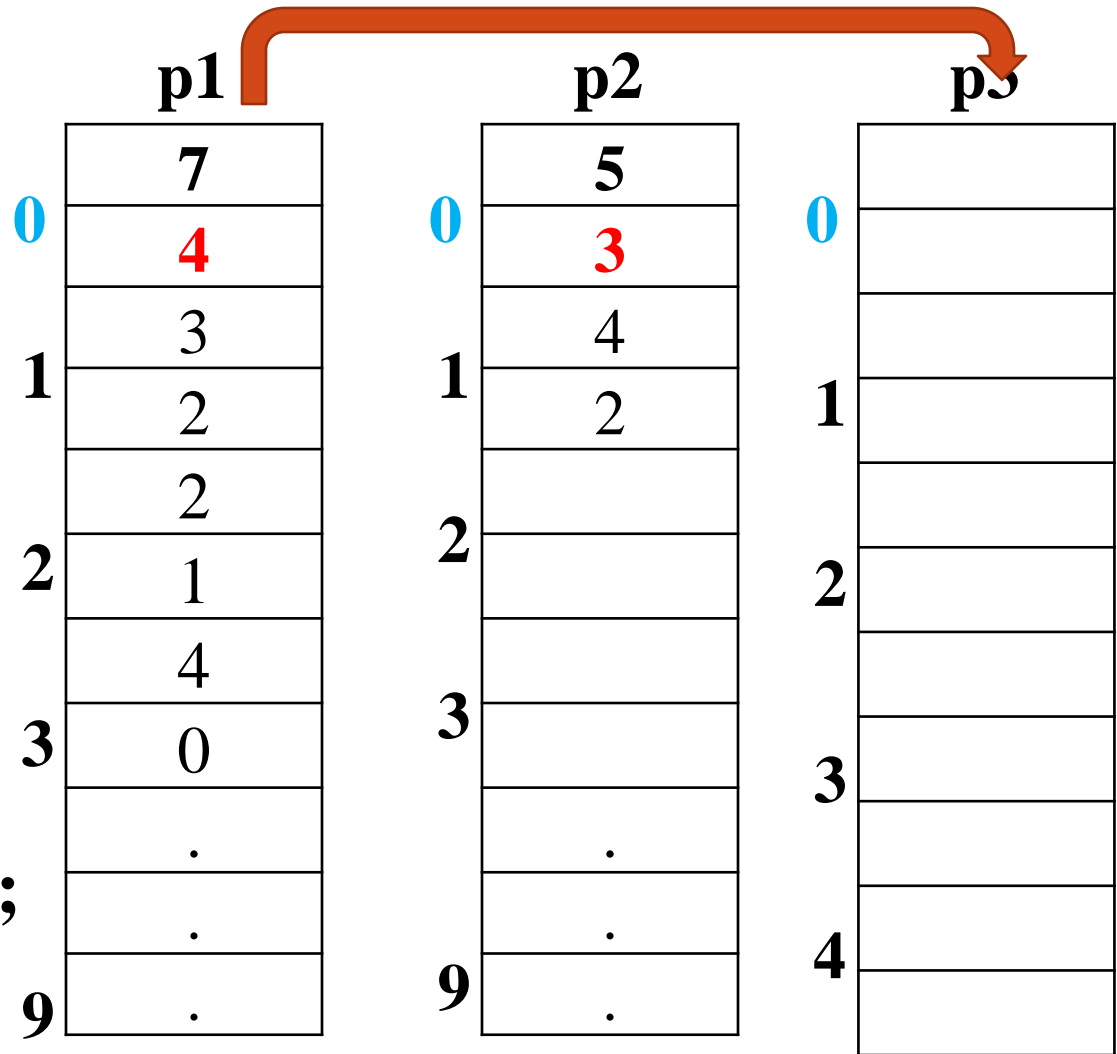
0	
1	
2	
3	
4	

POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

```

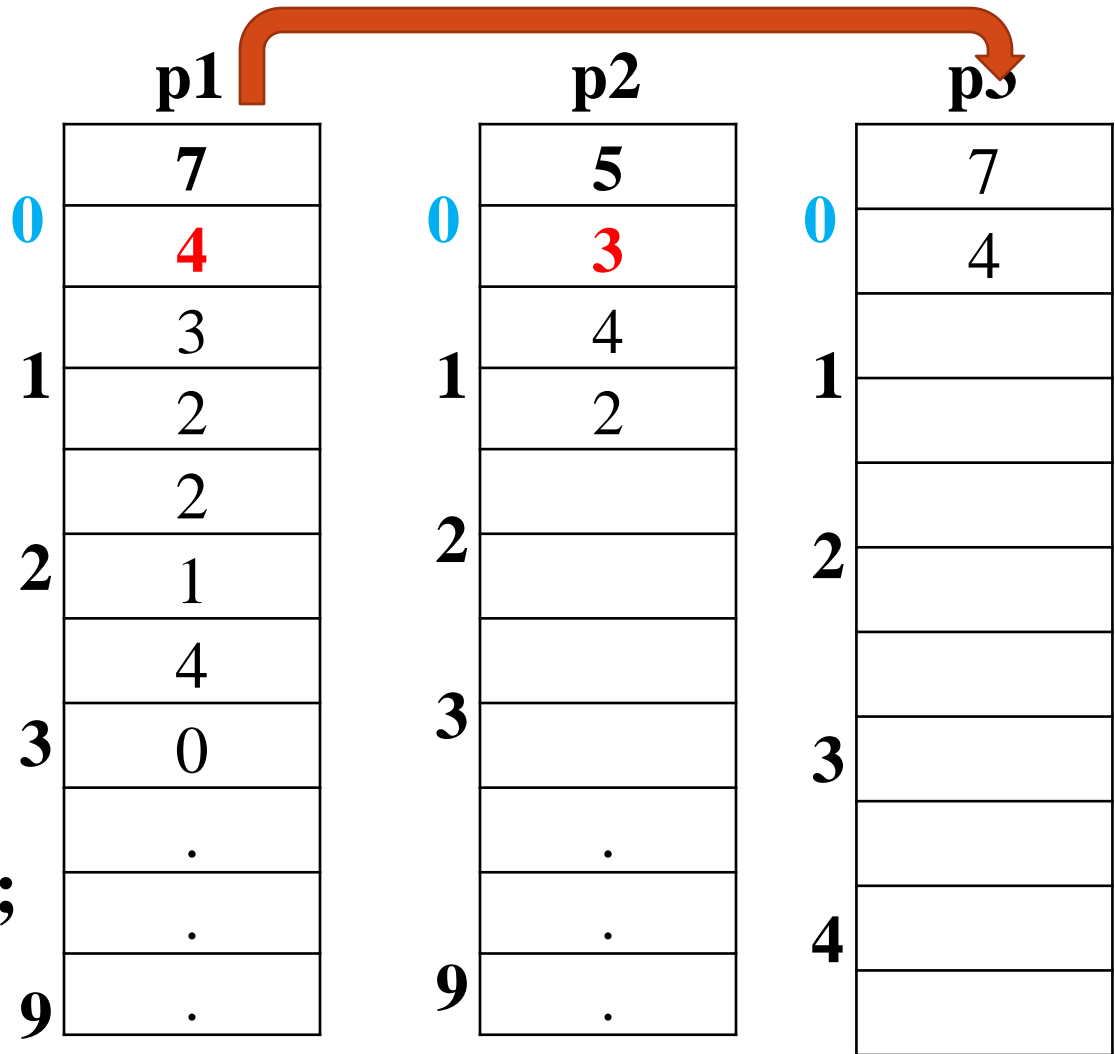
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```



POLYNOMIAL ADDITION USING ARRAY

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```



POLYNOMIAL ADDITION USING ARRAY

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- $5x^3 + 4x^2$

struct poly

{

int coeff;

int expo;

}p1[10],p2[10],p3[10];

p1

0	7
	4
1	3
	2
	2
2	1
	4
3	0
	.
	.
9	.

p2

0	5
	3
	4
1	2
2	
3	
	.
	.
9	.

p3

0	7
	4
1	
2	
3	
4	

POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

struct poly

{

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p1

0	7
	4
1	3
	2
2	2
	1
3	4
	0
	.
	.
9	.

p2

0	5
	3
1	4
	2
2	
3	
	.
	.
9	.

p3

0	7
	4
1	
2	
3	
4	

POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

struct poly

{

int coeff;

int expo;

}p1[10],p2[10],p3[10];

p1

0	7
	4
1	3
	2
2	2
	1
3	4
	0
	.
	.
9	.

p2

0	5
	3
1	4
	2
2	
3	
	.
	.
9	.

p3

0	7
	4
1	5
	3
2	
3	
4	

POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

struct poly

{

int coeff;

int expo;

}p1[10],p2[10],p3[10];

p1

0	7
	4
1	3
	2
2	1
	4
3	0
	.
	.
9	.

p2

0	5
	3
1	4
	2
2	
3	
	.
	.
9	.

p3

0	7
	4
1	5
	3
2	
3	
4	

POLYNOMIAL ADDITION USING

ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

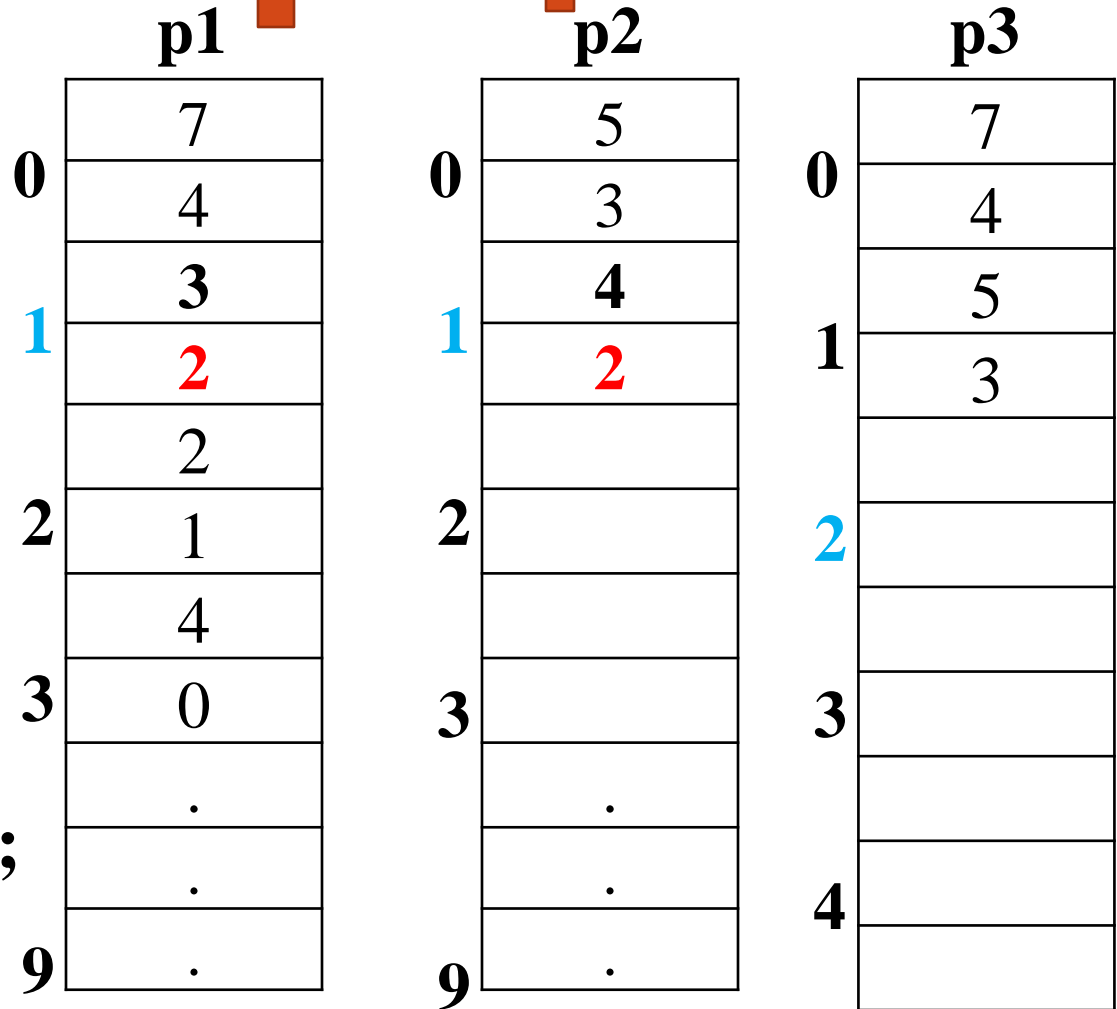
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POLYNOMIAL ADDITION USING

ARRAY

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- $5x^3 + 4x^2$

struct poly

{

int coeff;

int expo;

}p1[10],p2[10],p3[10];

p1

0	7
	4
1	3
	2
2	1
	4
3	0
	.
	.
9	.

p2

0	5
	3
1	4
	2
2	
3	
	.
	.
9	.

p3

0	7
	4
1	5
	3
2	7
	2
3	
4	



POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

struct poly

{

int coeff;

int expo;

}p1[10],p2[10],p3[10];

p1

0	7
	4
1	3
	2
	2
2	1
	4
3	0
	.
	.
9	.

p2

0	5
	3
1	4
	2
2	
3	
	.
	.
9	.

p3

0	7
	4
1	5
	3
	7
2	2
3	
4	

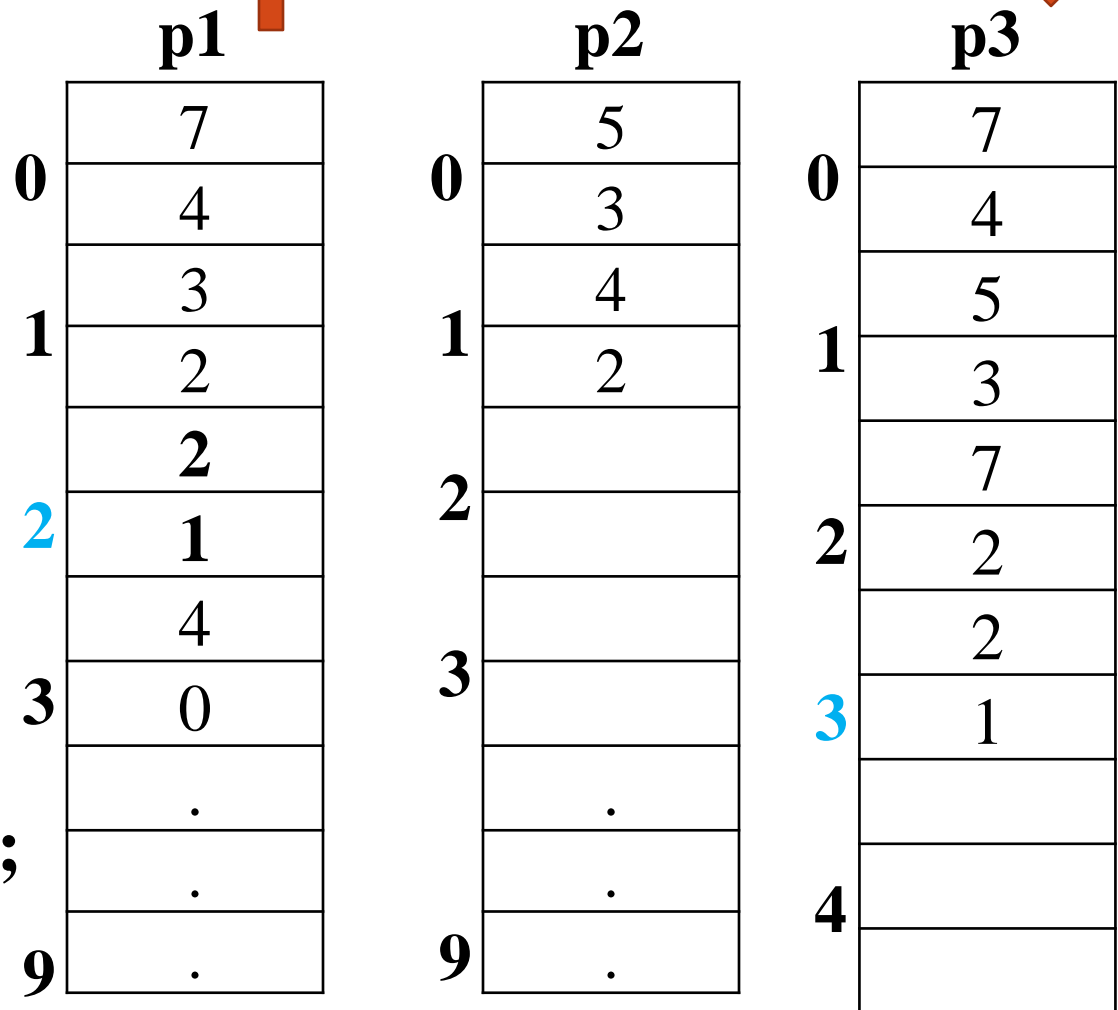


POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

```

struct poly
{
    int coeff;
    int expo;
}p1[10],p2[10],p3[10];
    
```

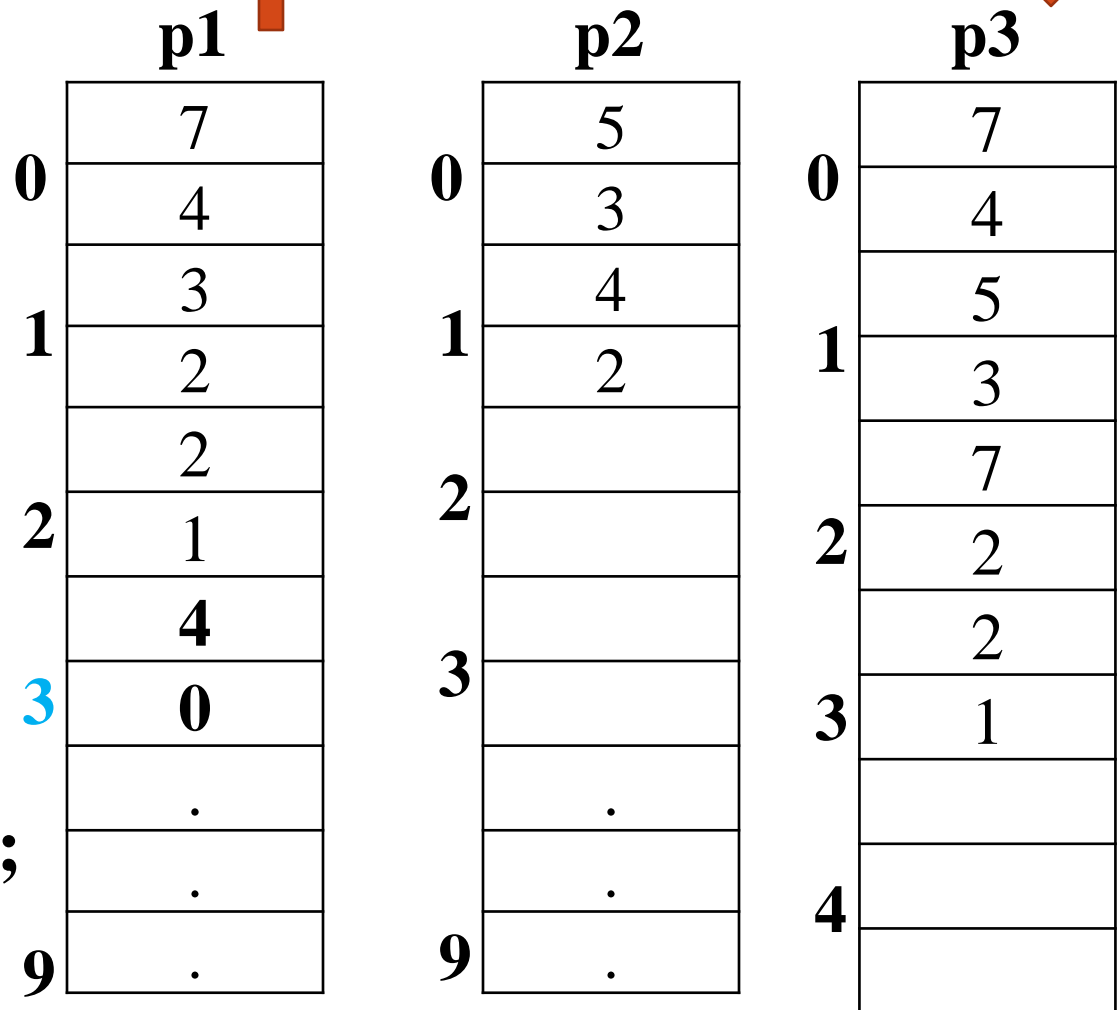


POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

```

struct poly
{
    int coeff;
    int expo;
}p1[10],p2[10],p3[10];
    
```



POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$
- $5x^3 + 4x^2$

struct poly

{

int coeff;

int expo;

}p1[10],p2[10],p3[10];

p1

0	7
	4
1	3
	2
	2
2	1
	4
3	0
	.
	.
9	.

p2

0	5
	3
1	4
	2
2	
3	
	.
	.
9	.

p3

0	7
	4
1	5
	3
	7
2	2
	2
3	1
	4
4	0



POLYNOMIAL ADDITION USING ARRAY

- $7x^4 + 3x^2 + 2x + 4$

- $5x^3 + 4x^2$

- **Sum = $7x^4 + 5x^3 + 7x^2 + 2x^1 + 4x^0$**

	p3
0	7
	4
1	5
	3
	7
2	2
	2
3	1
	4
4	0

Polynomial Addition- Algorithm

Algorithm main()

{

Declare a structure to keep the coefficient and exponent of polynomial

Declare structure arrays p1[10],p2[10],p3[10]

call t1=readPoly(p1)

call displayPoly(p1,t1)

call t2=readPoly(p2)

call displayPoly(p2,t2)

call t3=addPoly(p1,p2,t1,t2)

call displayPoly(p3,t3)

}

Polynomial Addition- Algorithm

Algorithm readPoly(p)

{

 Read t, the number of terms of the polynomial

 for i=0 to t-1 do

 read p[i].coeff and p[i].expo

 return t

}

Algorithm displayPoly(p,t)

{

 for i=0 to t-1 do

 display p[i].coeff , "(x^" ,p[i].expo ")+"

}

Algorithm addPoly(p1,p2,t1,t2,p3)

```
{  i=0,j=0,k=0
  while i<t1 && j<t2 do
  {  if p1[i].expo==p2[j].expo then
    {  p3[k].coeff=p1[i].coeff + p2[j].coeff
      p3[k].expo=p1[i].expo
      i=i+1
      j=j+1
      k=k+1
    }
    else if p1[i].expo>p2[j].expo then
    {  p3[k].coeff=p1[i].coeff
      p3[k].expo=p1[i].expo
      i=i+1
      k=k+1
    }
  }
```

```
else
{
    p3[k].coeff=p2[j].coeff
    p3[k].expo=p2[j].expo
    j=j+1          k=k+1
}
}
while i<t1 do
{
    p3[k].coeff=p1[i].coeff
    p3[k].expo=p1[i].expo
    i=i+1          k=k+1
}
while j<t2 do
{
    p3[k].coeff=p2[j].coeff
    p3[k].expo=p2[j].expo
    j=j+1          k=k+1
}
return(k)
```

Polynomial Addition- Program

```
struct poly
```

```
{
```

```
    int coeff;
```

```
    int expo;
```

```
}p1[10],p2[10],p3[10];
```

```
int readPoly(struct poly []);
```

```
int addPoly(struct poly [],struct poly [],int ,int ,struct poly []);
```

```
void displayPoly(struct poly [],int terms);
```

```
void main()
```

```
{   int t1,t2,t3;
```

```
    t1=readPoly(p1);
```

```
    printf("\nFirst polynomial : ");
```

```
    displayPoly(p1,t1);
```

```
    t2=readPoly(p2);
```

```
    printf("\nSecond polynomial : ");
```

```
    displayPoly(p2,t2);
```

```
    /* add two polynomials and display resultant polynomial */
```

```
    t3=addPoly(p1,p2,t1,t2,p3);
```

```
    printf("\n\nResultant polynomial after addition : ");
```

```
    displayPoly(p3,t3);
```

```
}
```

```
int readPoly(struct poly p[10])
{   int t1,i;

    printf("\nEnter the total number of terms in the polynomial:");
    scanf("%d",&t1);

    printf("\nEnter the COEFFICIENT and EXPONENT in
    DESCENDING ORDER\n");
    for(i=0;i<t1;i++)
    {   printf("  Enter the Coefficient(%d): ",i+1);
        scanf("%d",&p[i].coeff);
        printf("      Enter the exponent(%d): ",i+1);
        scanf("%d",&p[i].expo);
    }
    return(t1);
}
```

```
void displayPoly(struct poly p[10],int term)
{
    int k;
    for(k=0;k<term-1;k++)
        printf("%d(x^%d)+",p[k].coeff,p[k].expo);

    printf("%d(x^%d)",p[term-1].coeff,p[term-1].expo);
}
```



```
int addPoly(struct poly p1[10],struct poly p2[10],int t1,int t2,struct poly p3[10])
{
    int i=0,j=0,k=0;
    while(i<t1 && j<t2)
    {
        if(p1[i].expo==p2[j].expo)
        {
            p3[k].coeff=p1[i].coeff + p2[j].coeff;
            p3[k].expo=p1[i].expo;
            i++;    j++;    k++;
        }
        else if(p1[i].expo>p2[j].expo)
        {
            p3[k].coeff=p1[i].coeff;
            p3[k].expo=p1[i].expo;
            i++;    k++;
        }
        else
        {
            p3[k].coeff=p2[j].coeff;
            p3[k].expo=p2[j].expo;
            j++;    k++;
        }
    }
}
```

```
/* for rest over terms of polynomial 1 */
```

```
while(i<t1)
```

```
{
```

```
    p3[k].coeff=p1[i].coeff;
```

```
    p3[k].expo=p1[i].expo;
```

```
    i++;    k++;
```

```
}
```

```
/* for rest over terms of polynomial 2 */
```

```
while(j<t2)
```

```
{
```

```
    p3[k].coeff=p2[j].coeff;
```

```
    p3[k].expo=p2[j].expo;
```

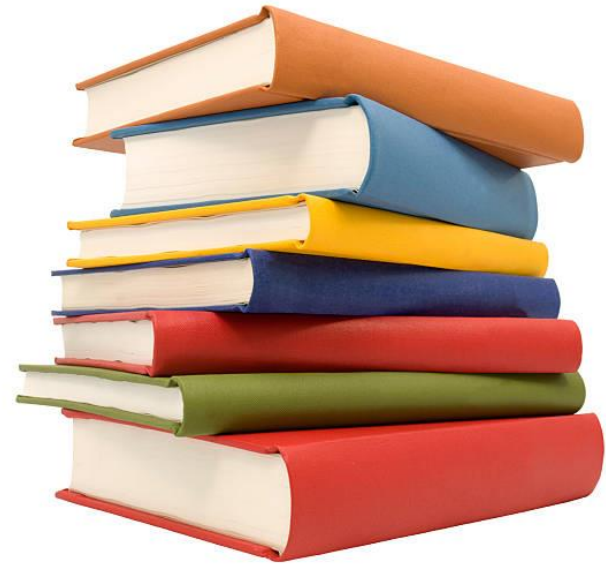
```
    j++;    k++;
```

```
}
```

```
return(k);    /* k is number of terms in resultant polynomial*/
```

```
}
```

STACK



- Stack is a linear data structure
- In case of array , insertion and deletion take place at any position
- Stack is an ordered collection of homogenous data elements where the **insertion and deletion operation takes place at one end only**
- It is a **Last in First Out (LIFO)** memory

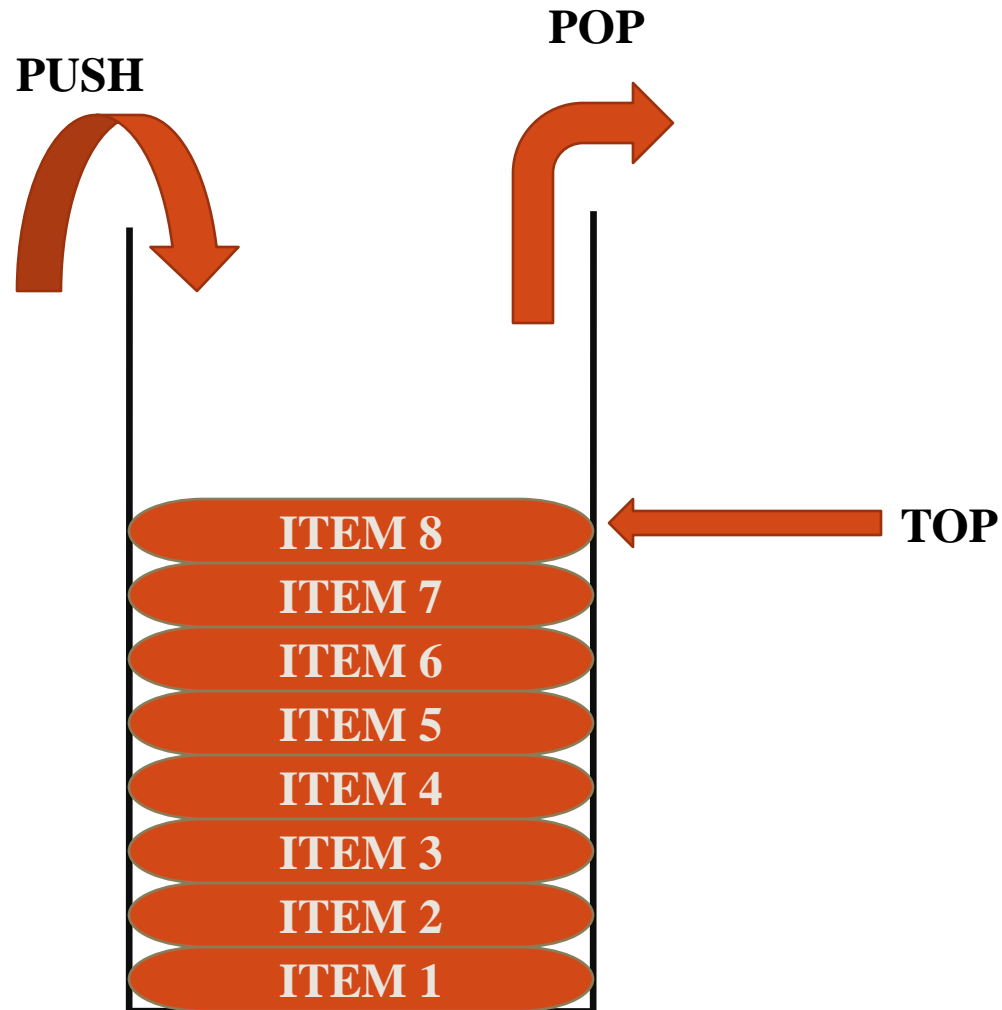
OPERATIONS ON STACK

- **PUSH**- Insert an element into the stack
- **POP**- Delete an element from the stack
- **STATUS**- To Know the present state of stack
- **DISPLAY** – To display the elements of the stack

Some Terminologies

- **TOP**- Position of the stack where PUSH and POP operations are performed
- **ITEM** – An element in a stack
- **SIZE** – Maximum number of elements that a stack can accommodate

STACK



STACK

- **Real time examples:**
 - Trains in a railway yard
 - Shipment of cargo

- **Applications of Stack:**
 - Evaluation of Arithmetic Expressions
 - Implementation of Recursion

REPRESENTATION OF STACK IN MEMORY

Two representations:

1. Array Representation
2. Linked List Representation

STACK DATA STRUCTURE ALGORITHMS

STACK REPRESENTATION USING ARRAY

```
int A[5];
```

If TOP == -1

Stack is EMPTY

A

4	
3	
2	
1	
0	

← **TOP = -1**

PUSH ITEM1

A

4	
3	
2	
1	
0	

← TOP = -1

TOP=TOP+1

A[TOP]=ITEM1

PUSH ITEM1

A

4	
3	
2	
1	
0	

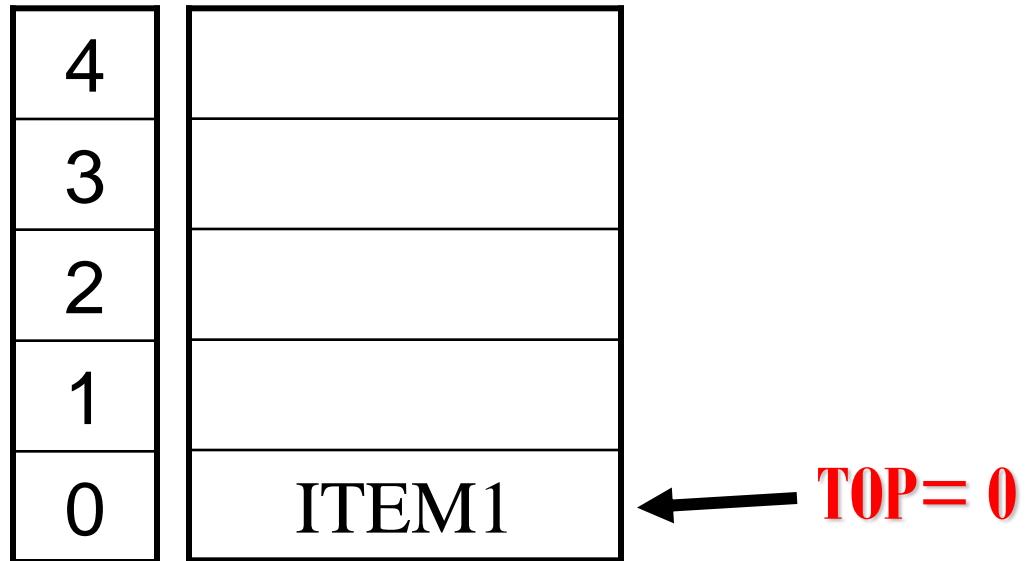
← TOP = -1

TOP=TOP+1

A[TOP]=ITEM1

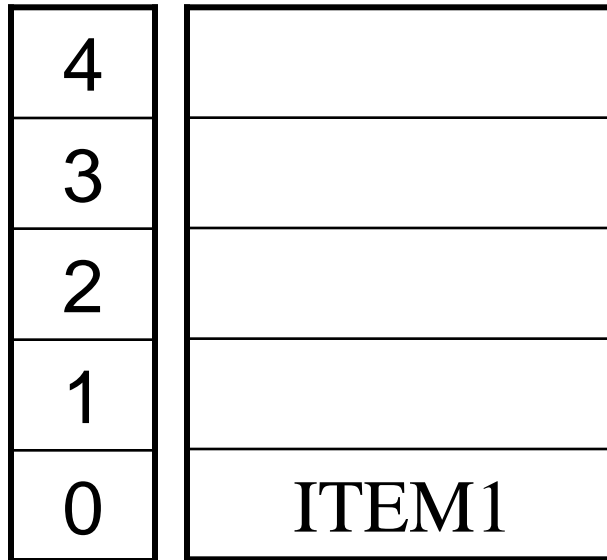
PUSH ITEM1

A



PUSH ITEM2

A



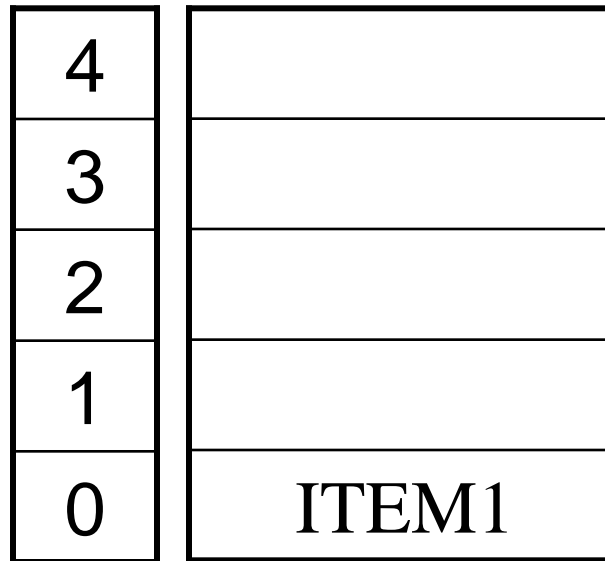
← TOP = 0

TOP=TOP+1

A[TOP]=ITEM2

PUSH ITEM2

A



← TOP = 0

TOP=TOP+1

A[TOP]=ITEM2

PUSH ITEM2

A

4	
3	
2	
1	ITEM2
0	ITEM1

← TOP = 1

PUSH ITEM3

A

4	
3	
2	
1	ITEM2
0	ITEM1

← TOP = 1

TOP=TOP+1

A[TOP]=ITEM3

PUSH ITEM3

A

4	
3	
2	
1	ITEM2
0	ITEM1

← TOP = 1

TOP=TOP+1

A[TOP]=ITEM3

PUSH ITEM3

A

4	
3	
2	ITEM3
1	ITEM2
0	ITEM1

← TOP = 2

PUSH ITEM4

A

4	
3	
2	ITEM3
1	ITEM2
0	ITEM1

← TOP = 2

TOP=TOP+1

A[TOP]=ITEM4

PUSH ITEM4

A

4	
3	
2	ITEM3
1	ITEM2
0	ITEM1

← TOP = 2

TOP=TOP+1

A[TOP]=ITEM4

PUSH ITEM4

A

4	
3	ITEM4
2	ITEM3
1	ITEM2
0	ITEM1

← TOP = 3

PUSH ITEM5

A

4	
3	ITEM4
2	ITEM3
1	ITEM2
0	ITEM1

← TOP = 3

TOP=TOP+1

A[TOP]=ITEM5

PUSH ITEM5

A

4	
3	ITEM4
2	ITEM3
1	ITEM2
0	ITEM1

← TOP = 3

TOP=TOP+1

A[TOP]=ITEM5

PUSH ITEM5

A

4	ITEM5
3	ITEM4
2	ITEM3
1	ITEM2
0	ITEM1

← TOP = 4

PUSH ITEM6

A

4	ITEM5
3	ITEM4
2	ITEM3
1	ITEM2
0	ITEM1

← TOP = 4

If $TOP=SIZE-1$
then

Stack is full

A

PUSH ITEM6

4	ITEM5
3	ITEM4
2	ITEM3
1	ITEM2
0	ITEM1

← **TOP = 4**

STACK – PUSH ALGORITHM

Algorithm PUSH(ITEM)

```
{  
    if TOP = SIZE – 1 then  
        Print “Stack is FULL”  
    else  
        {  
            TOP=TOP+1  
            A[TOP] = ITEM  
        }  
}
```

POP

A

4	ITEM5
3	ITEM4
2	ITEM3
1	ITEM2
0	ITEM1

← TOP = 4

ITEM=A[TOP]

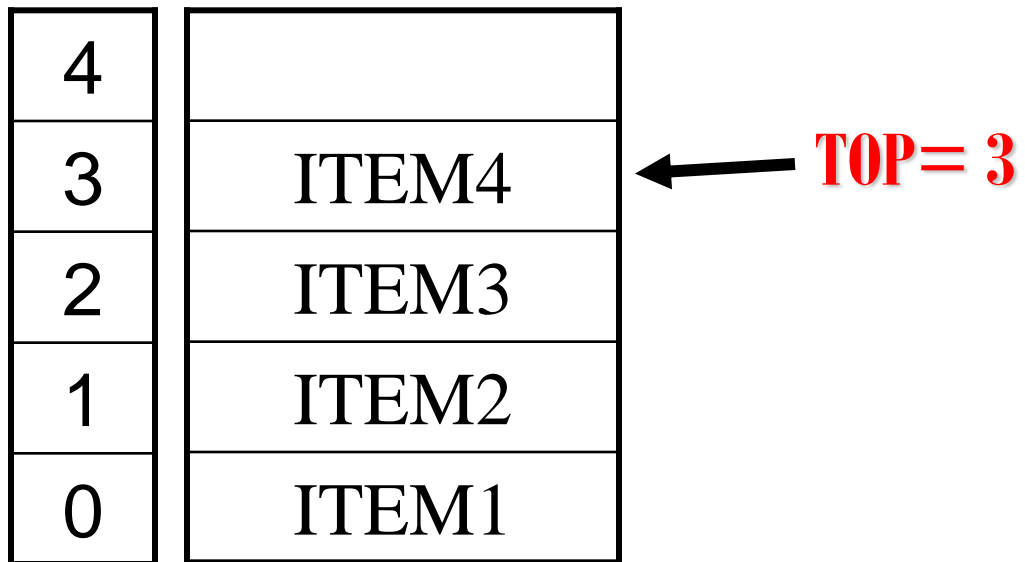
TOP=TOP-1

A

POP

4	ITEM5	← TOP = 4
3	ITEM4	
2	ITEM3	
1	ITEM2	
0	ITEM1	

A



POP

A

4	
3	ITEM4
2	ITEM3
1	ITEM2
0	ITEM1

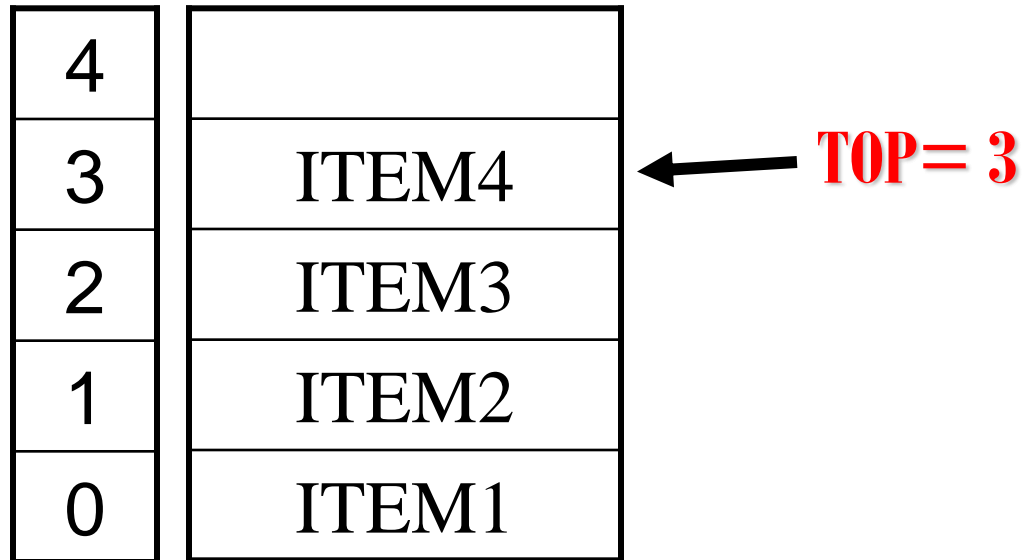
← TOP = 3

ITEM=A[TOP]

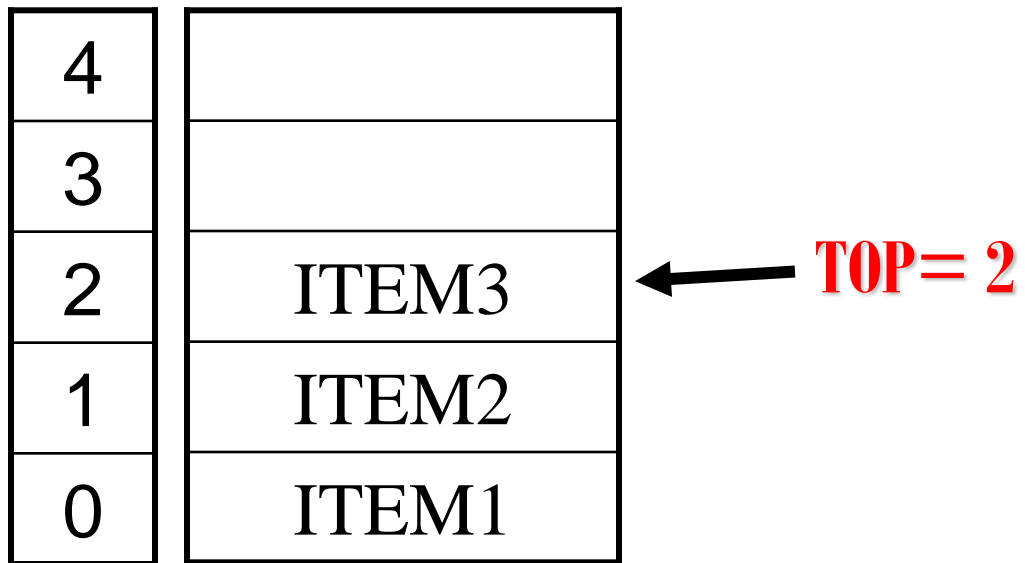
TOP=TOP-1

A

POP



A



POP

A

4	
3	
2	ITEM3
1	ITEM2
0	ITEM1

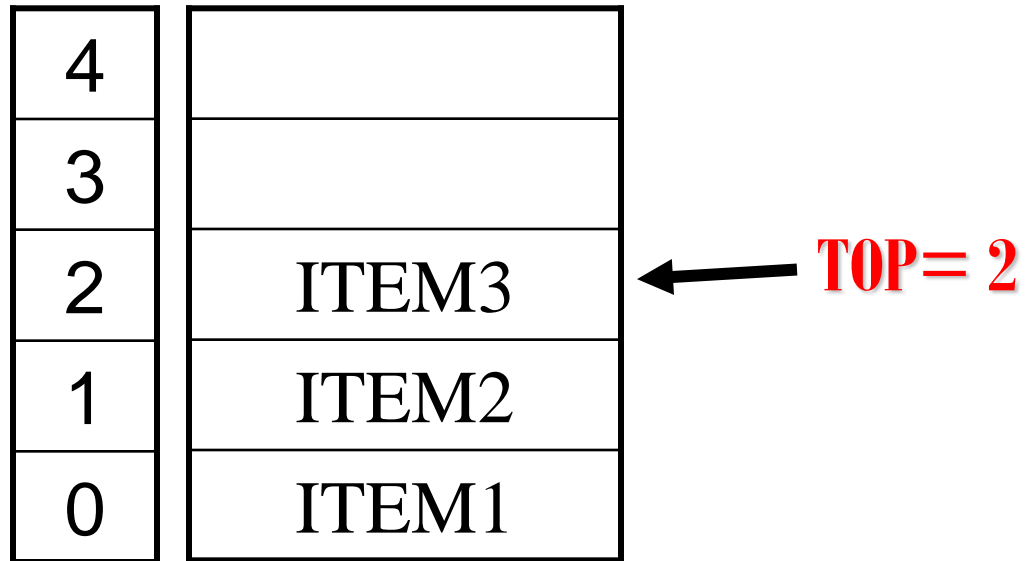
← TOP = 2

ITEM=A[TOP]

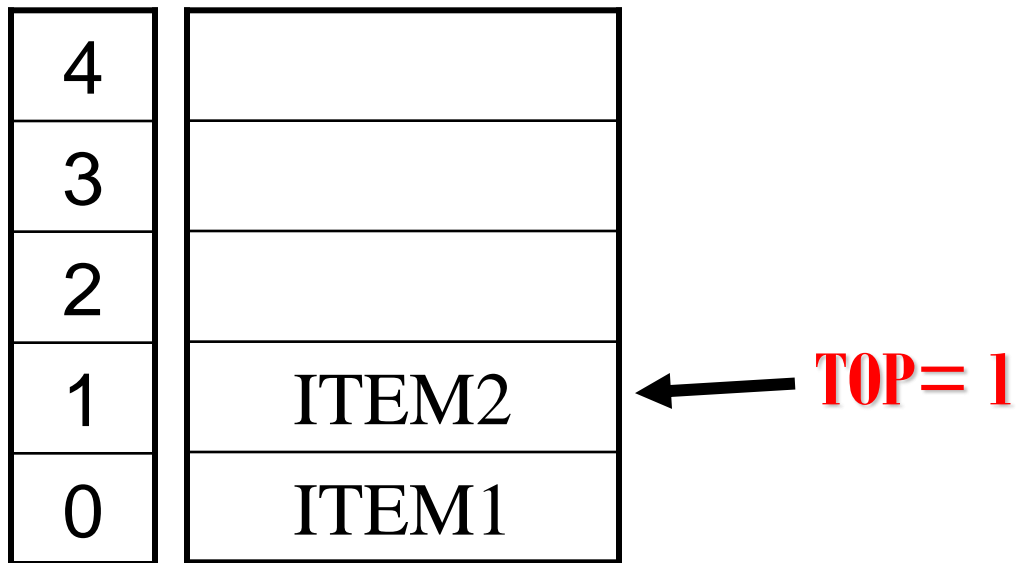
TOP=TOP-1

POP

A



A



POP

A

4	
3	
2	
1	ITEM2
0	ITEM1

← TOP = 1

ITEM=A[TOP]

TOP=TOP-1

POP

A

4	
3	
2	
1	ITEM2
0	ITEM1

← TOP = 1

A

4	
3	
2	
1	
0	ITEM1

← TOP = 0

POP

A

4	
3	
2	
1	
0	ITEM1

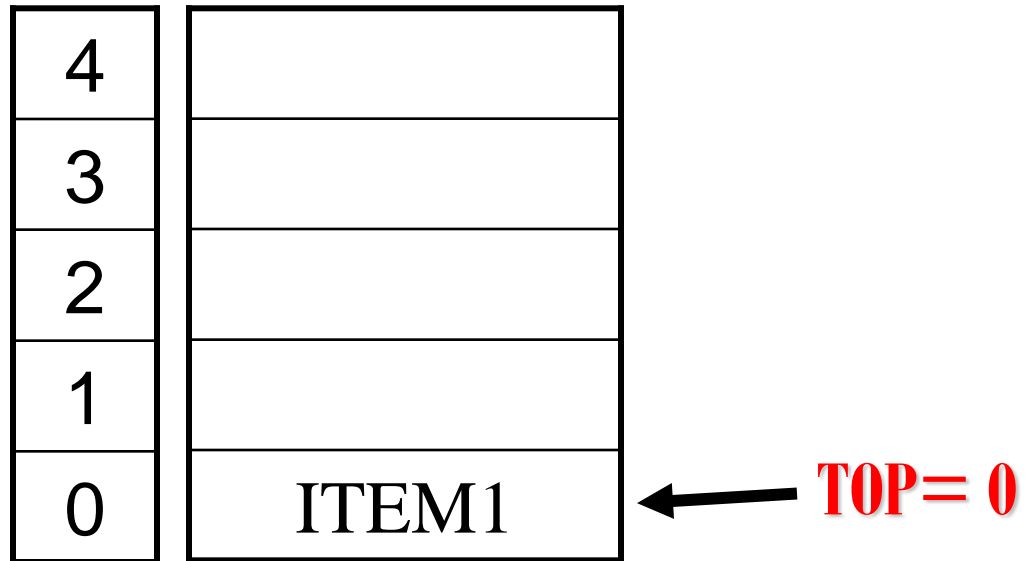
← TOP = 0

ITEM=A[TOP]

TOP=TOP-1

A

POP



A

4	
3	
2	
1	
0	

← TOP = -1

POP

A

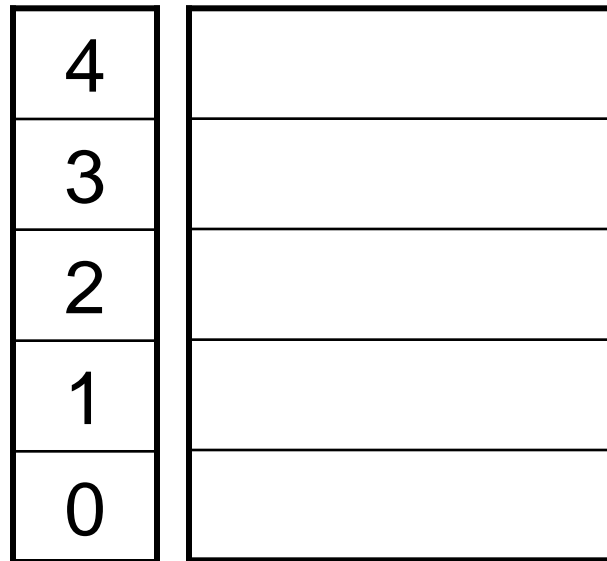
4	
3	
2	
1	
0	

← TOP = -1

If TOP == -1 then

Stack is empty

A



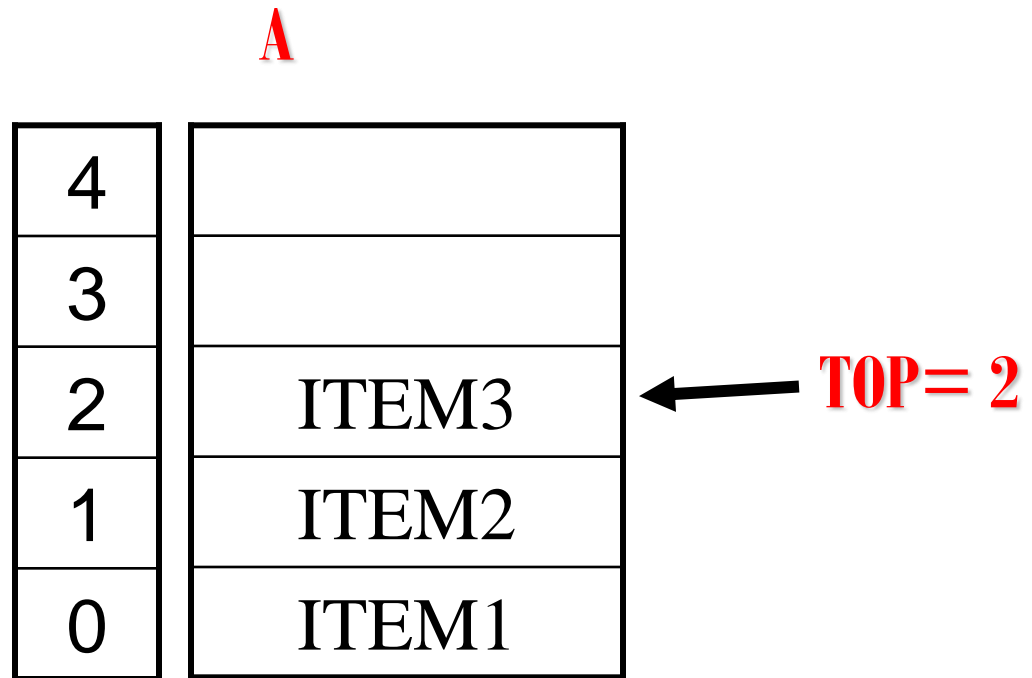
← TOP = -1

STACK – POP ALGORITHM

Algorithm POP()

```
{  
    if TOP = -1 then  
        Print “Stack is empty”  
    else  
        {  
            ITEM = A[TOP]  
            TOP=TOP-1  
            Print “Item to be popped is “ ITEM  
        }  
}
```

Display the contents of the stack from A[0] to A[TOP]



STACK – DISPLAY ALGORITHM

Algorithm DISPLAY()

```
{  
    if TOP = -1 then  
        Print "Stack is empty"  
    else  
        {  
            for i=0 to TOP do  
                Print A[i]  
        }  
}
```


STACK – STATUS ALGORITHM

Algorithm STATUS()

```
{   if TOP = -1 then
        Print “Stack is empty”
    else
        {   Print “Stack top element is ” A[TOP]
            if TOP=SIZE-1 then
                    Print “Stack is full”
                else
                    {   free=((SIZE-TOP-1)/SIZE)x100
                        Print “Free space is “ free
                    }
            }
    }
}
```

Implement Stack using Array

```
#include<stdio.h>
int A[100],size,top;
void push(int item)
{   if(top==size-1)
        printf("\nSTACK is full");
    else
    {       top++;
            A[top]=item;
    }
}
```

```
void pop()
{
    if(top==-1)
        printf("\nStack is empty");
    else
    {
        printf("\nThe popped elements is %d",A[top]);
        top--;
    }
}
```

```
void display()
{
    int i;
    if(top==-1)
        printf("\nThe STACK is empty");
    else
    {
        printf("\nThe elements in STACK \n");
        for(i=0; i<=top; i++)
            printf("\n%d",A[i]);
    }
}
```

```
void status()
{
    float free;
    if(top==-1)
        printf("Stack is empty");
    else
    {
        printf("Stack top element is %d",A[top]);
        if(top==size-1)
            printf("\nStack is full");
        else
        {
            free=(float)(size-top-1)*100/size;
            printf("\nFree space=%f% ",free);
        }
    }
}
```

```
void main()
{
    int choice,n;
    top=-1;
    printf("\nEnter the size of STACK:");
    scanf("%d",&size);
    do
    {
        printf("\n1.PUSH\t2.POP\t3.DISPLAY\t
                4.STATUS\t5.EXIT");
        printf("\nEnter the Choice:");
        scanf("%d",&choice);
```

```
switch(choice)
{
    case 1:    printf("Enter a value to be pushed:");
              scanf("%d",&n);
              push(n);    break;
    case 2:    pop();      break;
    case 3:    display();  break;
    case 4:    status();   break;
    case 5:    break;
    default:   printf("\nPlease Enter a Valid Choice(1/2/3/4/5)");
}

}while(choice!=5);
} //end of main()
```